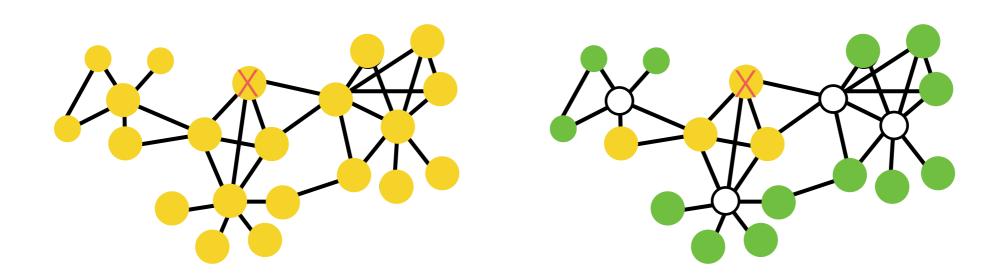


Removing nodes can have a number of effects:

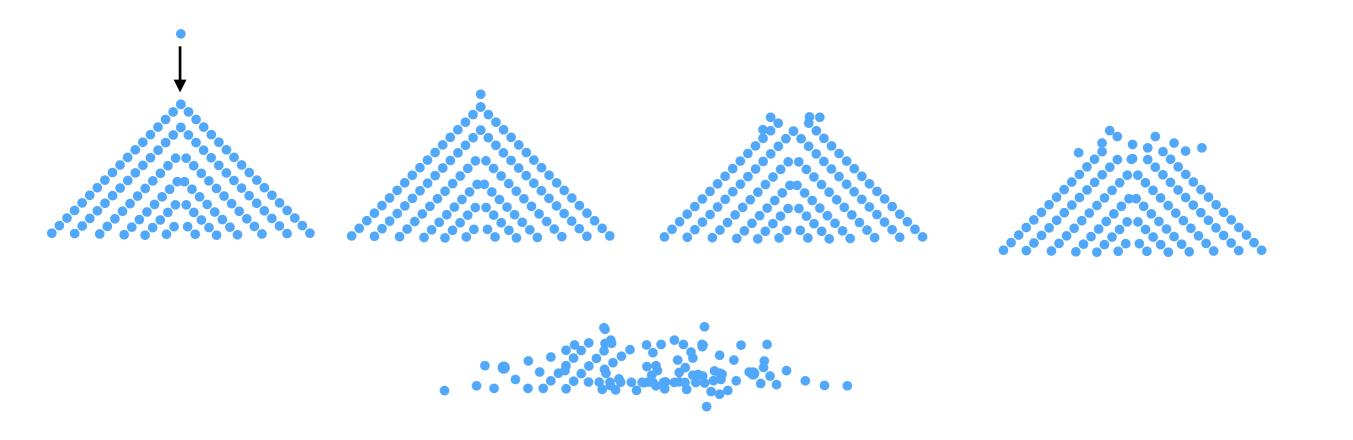
- Path length 1
- Average degree ↓
- Size of largest connected component ↓

This should sound familiar from when we looked at vaccinating individuals to prevent the spread of disease: "removing" nodes fragments the network



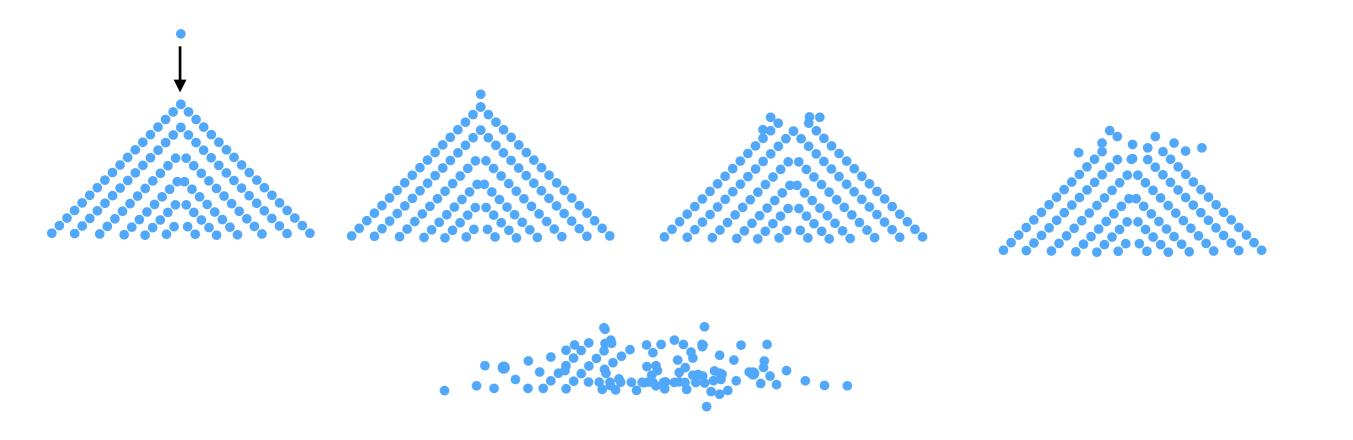
If nodes depend on each other, then there may be a chain reaction: removing one node may lead to others being removed as well

This process is called a *cascade* 



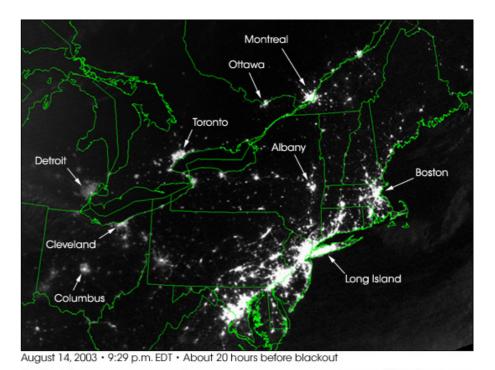
If nodes depend on each other, then there may be a chain reaction: removing one node may lead to others being removed as well

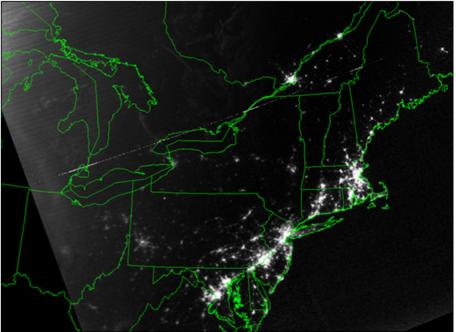
This process is called a *cascade* 



Cascading failure is important in many contexts:

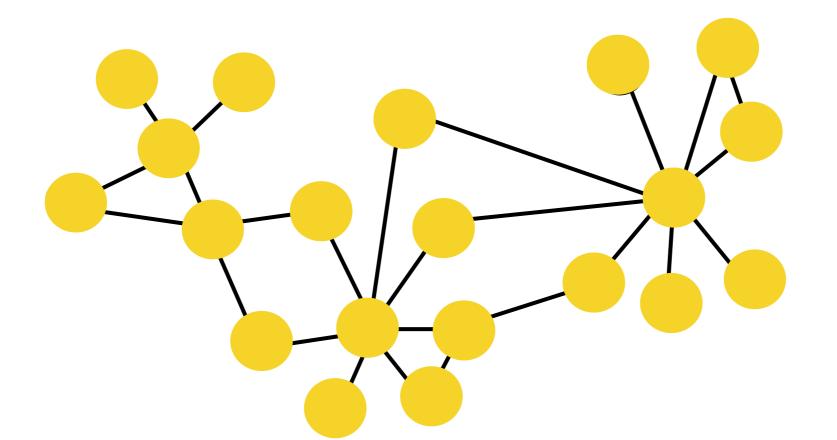
Servers Financial Systems City Traffic Power Grids Ecosystems Airline Traffic



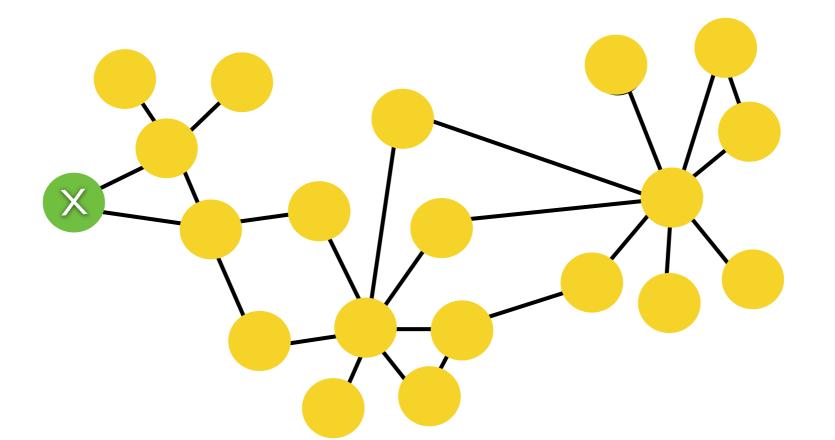


August 15, 2003 • 9:14 p.m. EDT • About 7 hours after blackout

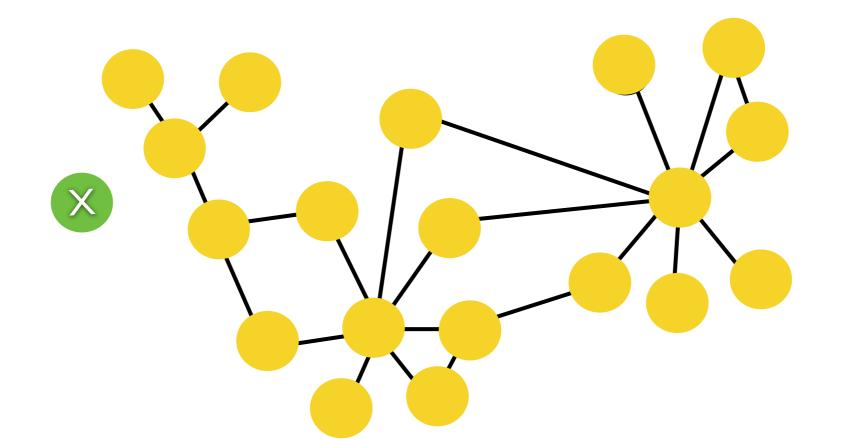
- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



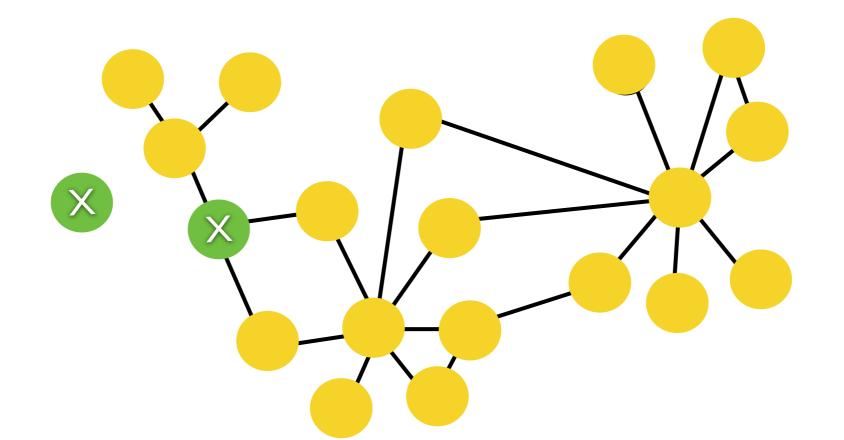
- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



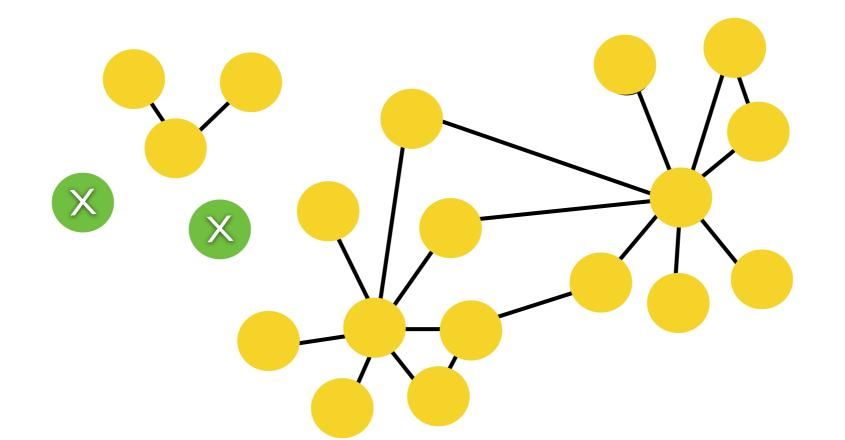
- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



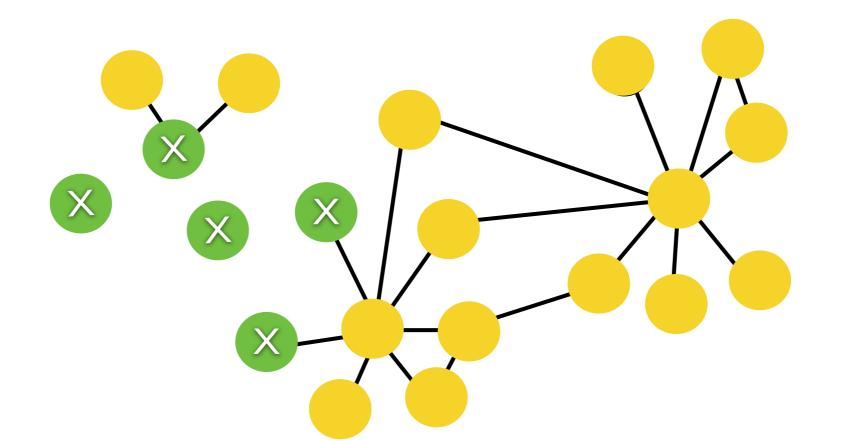
- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



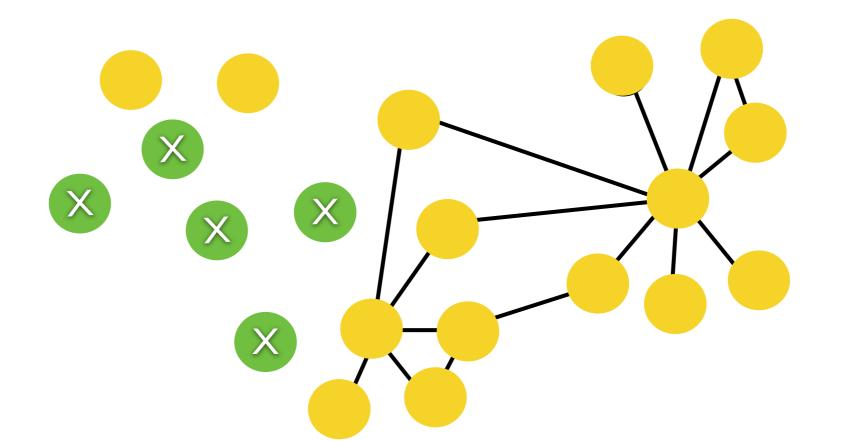
- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



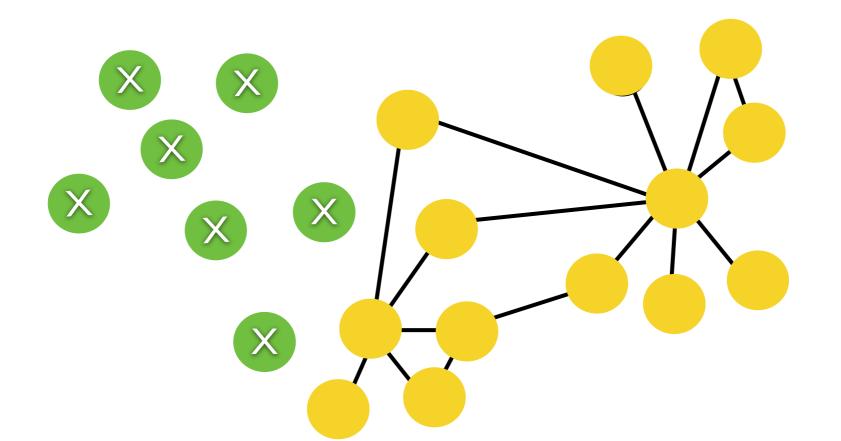
- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network

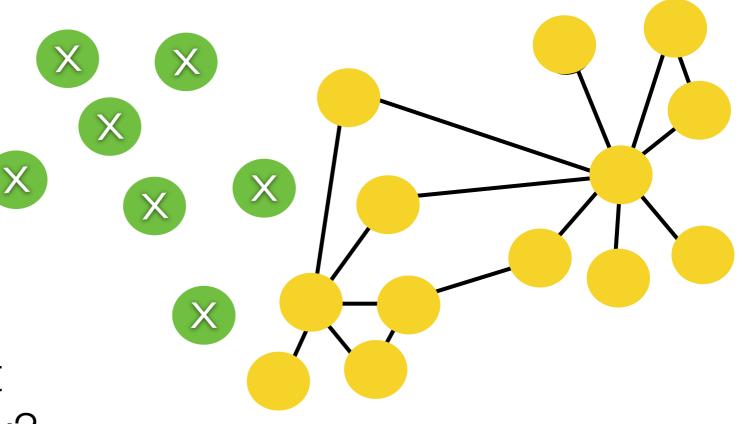


- If B fails, then they default on the loan to A
- If enough of A's investments fail, then they also default
- A default can spread through the network



So one failure can cause many failures—how many will depend on the structure of the network, and which node initially fails.

Question 1: what characteristics of the network affect it's resilience?

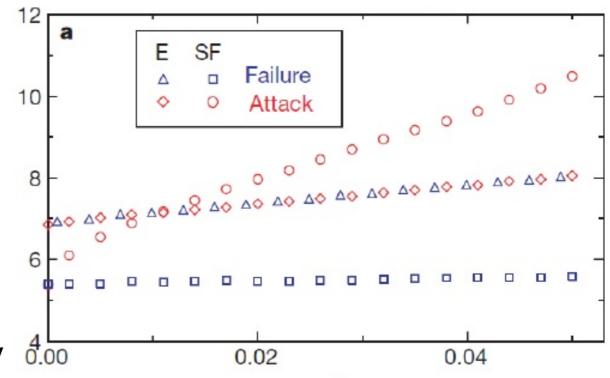


Question 2: how is a random failure different than a deliberate attack?

Characteristic 1: Degree distribution

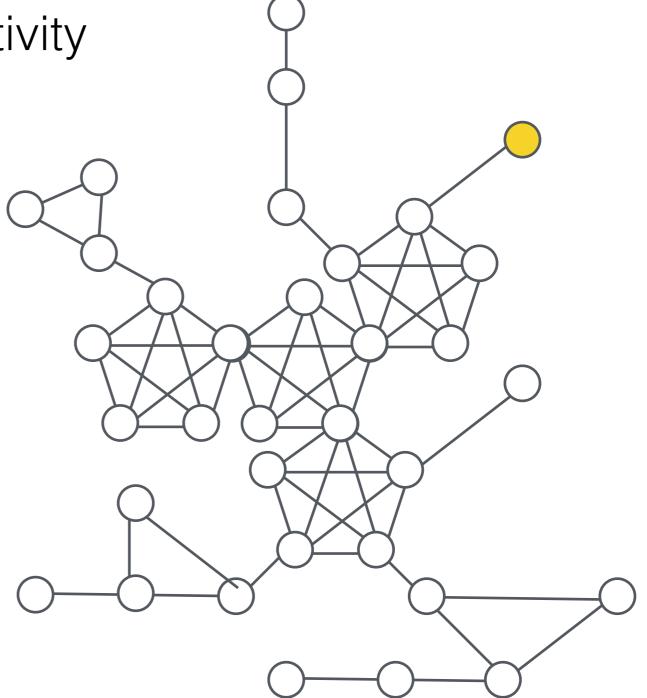
Higher average degree: less resilience to node deletion

More skewed degree distribution: less resilience to node deletion (generally speaking)



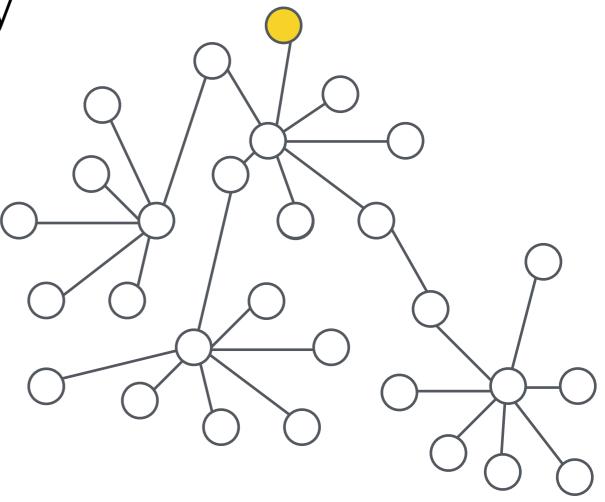
Characteristic 2: Assortativity

Assortative networks fail quickly, but the failure is not wide-spread

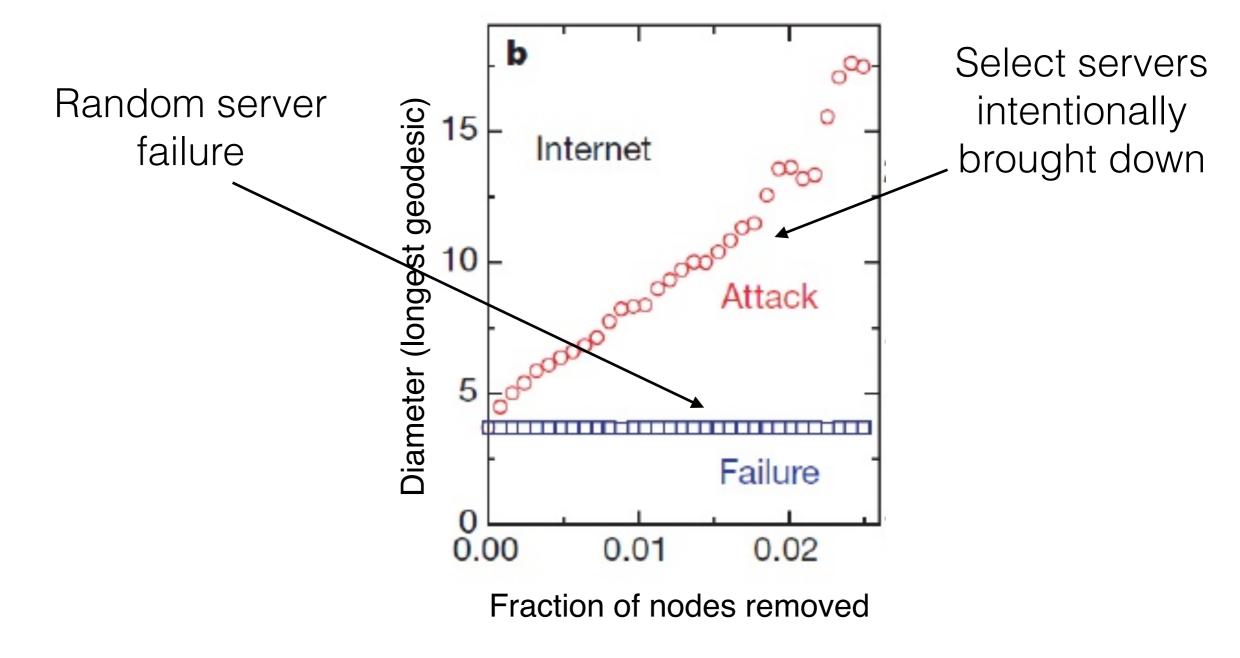


Characteristic 2: Assortativity

Disassortative networks fail slowly, but comprehensively



It also depends on whether the failure was random, or a deliberate choice



This has implications for how we should design power networks, airline routes, road systems, server networks, etc to prevent wide-spread failure due to terrorist attack

It also might have implications for how covert networks are formed to minimize the chances of the whole system going down at once